# SAMPLE QUESTION PAPER MATHEMATICS <br> Class X 

Time: 3 hrs
Marks: 80

## General Instructions

1. All questions are compulsory
2. The question paper consists of 25 questions divided in to three sections $A, B$ and $C$. Section $A$ contains 7 questions of 2 marks each .Section B is of 12 Questions of 3 marks each and section $C$ of 6 Questions of 5 marks each
3. There is no overall choice .However ,internal choice has been provided in two questions of two marks each, two questions of three marks each, two questions of five marks each
4. In question on construction, drawing should be neat exactly as per the given measurements.
5. Use of calculators is not permitted.

## SECTION - A

Q1. If $\mathbf{x}+\mathbf{3}$ is a factor of $\boldsymbol{x}^{3}+\boldsymbol{a} \boldsymbol{x}^{2}+\boldsymbol{b} \boldsymbol{x}+9$ and $\boldsymbol{a}+\boldsymbol{b}=\mathbf{1 4}$ find $\mathbf{a}$ and $\mathbf{b}$

Q2. If $(\mathbf{x}-\boldsymbol{\alpha})$ is the H.C.F of $\mathbf{x}^{2}+\mathbf{a x}+\mathbf{b}$ and $\mathbf{x}^{2}+\mathbf{b x}+\mathbf{a}$ then find the value of $\boldsymbol{\alpha}$ and also find the value of $\mathbf{a}+\mathbf{b}+\mathbf{1}$

Q3. A mixi is available for Rs $\mathbf{5 , 4 0 0}$ cash or Rs $\mathbf{1 , 4 0 0}$ cash down payment followed by Rs $\mathbf{4 , 2 4 0}$ after $\mathbf{6}$ months. .Find the rate of interest charged under this instalment scheme.

Q4. Cards marked with all 2-digit numbers are placed in a box and thoroughly mixed up. One card is picked at random. Find the probability of getting
(i) A number divisible by 10
(ii) A perfect square

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Q5. What is the difference between the $\mathbf{2 0}^{\text {th }}$ terms of two AP with same common difference and first terms $\mathbf{3}$ and $\mathbf{8}$ ? Justify your answer.

OR
Find the number of terms of the AP 54, 51, 48 ... so that their sum is 513.
Q6. Solve for x
$4 x^{2}+2(a-b) x-a b=0$

## OR

Solve for x :
$x^{2}-4 a x+4 a^{2}-b^{2}=0$

Q7. Prove that a cyclic parallelogram is a rectangle.

## SECTION - B

Q8. The height of a cylinder is 15 cm . the curved surface area is $660 \mathrm{~cm}^{2}$. Find the radius .
OR
The circumference of the edge of a hemispherical bowl is 132 cm . find the capacity of the bowl

Q9. Express the following expression as a rational expression in its lowest terms
$\frac{x^{4}-8 x}{2 x^{2}+5 x-3} \times \frac{2 x-1}{x^{2}+2 x+4} \times \frac{x+3}{x^{2}-2 x}$

Q10. In a flight of $\mathbf{2 8 0 0} \mathbf{~ k m}$, an aircraft was slowed down due to bad weather. The average speed of the trip was reduced by $\mathbf{1 0 0} \mathbf{K m} / \mathbf{h r}$ and the time increased by $\mathbf{3 0}$ minutes. Find the original duration of the flight.

Q11. A computer is available for Rs $\mathbf{3 9 3 0 0}$ cash or for Rs $\mathbf{1 2 8 2 0}$ cash down payment and three equal half yearly installments .If the dealer charges interest at the rate of $20 \%$ per annum compounded semi annually, Calculate each installment

Q12. If $\mathrm{a}, \mathrm{b}, \mathrm{c}$ are $\mathrm{p}^{\text {th }}, \mathrm{q}^{\text {th }}, \mathrm{r}^{\text {th }}$ terms of an AP then prove that $a(q-r)+b(r-p)+c(p-q)=0$

Q13. In the given figure ABC is a triangle in which $\boldsymbol{A B}=\boldsymbol{A} \boldsymbol{C}$ $A$ circle through $B$ touches $A C$ at $D$ and intersects $A B$ at $P$.If $D$ is the mid point of $A C$, show that $\mathbf{4 A P}=\boldsymbol{A B}$


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Q14. Prove that $\frac{1+\cos \theta}{1-\cos \theta}=\frac{\tan ^{2} \theta}{(\sec \theta-1)^{2}}$
OR
Without using trigonometric table evaluate
$\frac{\operatorname{Cos} 58^{0}}{\operatorname{Sin} 32^{0}}+\frac{\operatorname{Sin} 22^{\circ}}{\operatorname{Cos} 68^{0}}-\frac{\operatorname{Cos} 38^{\circ} \operatorname{Cosec} 52^{\circ}}{\tan 18^{0} \tan 35^{0} \tan 60^{\circ} \tan 72^{0} \tan 55^{0}}$

Q15. Prove that the points $(\mathbf{- 2 , - 1}),(\mathbf{1 , 0}),(\mathbf{4}, \mathbf{3})$ and $(\mathbf{1}, \mathbf{2})$ are the vertices of parallelogram .Is it a rectangle.

Q16. A (-1, 0), B(1,2), C(5,-2) are the three vertices of a rectangle $A B C D$. Find the coordinates of the point D .

Q17. Mukesh's monthly salary is $\mathbf{R s} \mathbf{1 8 0 0 0}$. He plans his budget for a month as given below

| Item | Food | Rent | Education | Savings | Misc | Total |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Amount(Rs) | 5250 | 3500 | 3250 | 4000 | 200 | 18000 |

Represent the above data in a pie chart.

Q18. Construct $\triangle \mathrm{ABC}$ having perimeter $\mathbf{1 4} \mathbf{~ c m}$ and $\left\langle\boldsymbol{B}=\mathbf{6 0}^{\mathbf{0}},\left\langle\boldsymbol{A}=\mathbf{3 0}^{\mathbf{0}}\right.\right.$ then construct the circumcircle of the triangle.

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Q19. Solve the following system linear equations graphically $\quad \mathbf{3 x}-\mathbf{4 y}=\mathbf{1 2}, \mathbf{2 x}+\mathbf{y}-\mathbf{2}=\mathbf{0}$. Also find the coordinates of the points where the lines meet the X axis

## SECTION - C

Q20. Prove that in a right triangle, the square of the hypotenuse is equal to the sum of the squares of the other two sides.
Use the above theorem, to prove that

$$
\mathbf{P R}^{2}=\mathbf{P Q}^{2}+\mathbf{Q R}^{2}-2 \mathbf{Q M} . \mathrm{QR}
$$



Q21. If a line touches a circle and from the point of contact, a chord is drawn, show that the angles which the chord makes with the given line are respectively equal to the angles formed in the corresponding alternate segment. Using the above theorem, in fig PQ II AB, Given PQ is a tangent to the circle at X , Prove that $\mathbf{X A}=\mathbf{X B}$


Q22. A cone of height $\mathbf{1 5 ~ C m}$ and diameter $\mathbf{7 C m}$ is mounted on a hemisphere of the same diameter .Determine the volume of the solid thus formed .(use $\pi=\frac{22}{7}$ )

## OR

Find the number of bricks each measuring $25 \mathrm{Cm} \times 16 \mathrm{Cm} \times 10 \mathrm{Cm}$ required to construct a

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wall $\mathbf{2 4 m}$ long, $\mathbf{6 m}$ high and $\mathbf{0 . 4 m}$ thick The mortar occupies $\frac{1}{10}^{\text {th }}$ of the volume of the wall.

Q23. A person standing on the bank of a river observes that the angle of elevation of the top a tree standing on the opposite bank is $\mathbf{6 0}^{\mathbf{0}}$. When he moves 40 m away from the bank, he finds the angle of elevation to be $\mathbf{3 0}^{\mathbf{0}}$. Find the height of the tree and the width of the river

## OR

From the top of a building $\mathrm{AB}, \mathbf{6 0} \mathbf{~ m}$ high, the angles of depression of the top and bottom of a vertical lamp post $C D$ are observed to be $\mathbf{3 0}^{\circ}$ and $\mathbf{6 0}{ }^{\boldsymbol{0}}$ respectively find
(i) The horizontal distance between AD and CD .
(ii) The difference between the heights of the building and the lamp post.

Q24. The pie chart (as shown in the figure) represents the amount spent on different sports by a sports club in a year. If the amount spent by the club for hockey is $\mathbf{3 0 , 0 0 0}$.Find the total amount spent and amount spent on each sports


Q25. Monthly income of Mrs. Saritha, who is a Senior citizen, is Rs35000. She donates Rs 25000 Prime Minister's Relief Fund (100\% exemption) and Rs 20000 to a charitable society ( $50 \%$ exemption ) . She contributes Rs $\mathbf{6 0 0 0 0}$ towards PPF annually and pays a quarterly premium of Rs $\mathbf{4 5 0 0}$ towards life insurance. She also purchases NSC's for Rs 30000 .Find the amount she has to pay towards income tax for the financial year Use the following for calculating income tax
(a) Savings : 100\% exemption for Savings up to Rs 100000
(b) Rate of Income Tax for Senior Citizen :

| Slab | Income Tax |
| :--- | :--- |
| Up to 185000 | No tax |
| From 185000 to Rs 250000 | $20 \%$ of the taxable income above Rs 185000 |
| Above Rs 250000 | Rs $13000+30 \%$ of the income exceeding Rs |


(c) Education Cess : $2 \%$ of the income tax
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